

Special Issue

Journal of Computing Science and Engineering, Vol. 11, No. 4, December 2017, pp. 130-141

## Feature Selection Based on Bi-objective Differential Evolution

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### Abstract

Feature selection is one of the most challenging problems of pattern recognition and data mining. In this paper, a feature selection algorithm based on an improved version of binary differential evolution is proposed. The method simultaneously optimizes two feature selection criteria, namely, set approximation accuracy of rough set theory and relational algebra based derived score, in order to select the most relevant feature subset from an entire feature set. Superiority of the proposed method over other state-of-the-art methods is confirmed by experimental results, which is conducted over seven publicly available benchmark datasets of different characteristics such as a low number of objects with a high number of features.

Category: Databases / Data Mining

Keywords: Feature selection; Rough set theory; Differential evolution; Classification

### **I. INTRODUCTION**

Data mining is the kind of knowledge discovery process for searching meaningful patterns or interesting information from the real life voluminous dataset with a huge number of redundant, noisy and inconsistent data. Tremendous growth in technology in the past few decades results in a mammoth amount of data which is to be analyzed intelligently to extract fruitful knowledge from it. Feature selection is an important part of dimension reduction which is mainly done in two approaches: filter approach [1], which is independent of underlying classifier strategy, and wrapper approach [2], which entirely depends upon the underlying classifier. However, some hybrid feature selection [2] and embedded feature selection [3] techniques are noticeable in the literature. To overcome the curse of dimensionality [4], feature selection is the most important part of data mining. Objective of feature

#### Open Access http://dx.doi.org/10.5626/JCSE.2017.11.4.130

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Received 25 May 2017; Accepted 25 November 2017 \*Corresponding Author selection process is to select the most informative and compact subset from an entire feature set without losing any important information required for subsequent data mining process. Small sample size and external noise are often treated as obstacles for achieving good mining result from the data. The stability which indicates the insensitivity of feature selection over external perturbation in the data set or induced noise in the data set plays an important role in the knowledge discovery process.

Inherently, feature selection is a combinatorial optimization problem [5] which searches an optimal feature subset of a pool of 2<sup>N</sup> competing candidate subset in the data set of N features. Optimum feature selection can be done by means of several unsupervised measures like feature similarity measure (FSFS) [6], unsupervised discriminative feature selection (UDFS) [7], multi-cluster feature selection [8], etc. Popular methods for feature selection include the fuzzy-rough feature selection [9-11], rough set based feature selection [12, 13] and probabilistic feature selection [14]. Independent of learning mechanism to search for an optimal feature subset is the primary objective of feature selection algorithm. As optimal feature subset selection from a pool of 2<sup>N</sup> competing candidate solution is an NP-complete problem, several evolutionary search methods [15-20] are used for the purpose.

At present situation, differential evolution (DE) [21, 22] holds a very prominent role in evolutionary optimizer space. Various measures have been taken to improve the performance of DE for scalable optimization problems. Some DE-variants incorporate parameter adaptation based on success-history (like SaDE [23], JADE [24]), new mutation and crossover policies (like Pro-DE [25], MDE-pBX [26]), and combining diverse offspring generation policies (like CoDE [27], EPSDE [28]). For large-scale optimization problems (greater than 500 dimensions) DE has been adopted by methods including comprehensibly all the above three algorithmic philosophies. Owing to its inherent simplicity, DE was used as the base optimizer in Yang et al.'s first work [29] on random grouping based CCEAs. Zamuda et al. [30] enriched DE by log-normal self-adaptation of its control parameters and by using cooperative co-evolution as a decomposition mechanism based on each dimension. The cooperative micro-DE developed by Parsopoulos [31] for large scale global optimization. Zhao et al. [32] hybridized the self-adaptive DE with MTS for large scale optimization. Some other approaches of improving DE for high-dimensional function optimization can be found in [33-35].

In the paper, multi-objective search for optimal feature subset selection using bi-objective differential evolution is proposed. In the method, feature selector uses two objective functions, one based on set approximation accuracy of rough set theory [36] and the other based on division operation of relational algebra. For selection step in proposed modified binary differential evolution, a dominance based [37] approach is used in the paper. Each bi-objective differential evolution based feature selector (DEFS) produces a non-dominated [37] feature subset from which the final feature subset is chosen. Some wellknown datasets with typical characteristics like small sample size with large feature size, and large sample size with small feature size are collected from publicly available UCI ML repository [38] to show the effectiveness of the proposed method. Performance comparison of proposed method with some state of the art feature selection methods like feature similarity measure or FSFS [4], Laplacian score for feature selection or LSFS [39], multi-cluster feature selection or MCFS [40], dense subgraph finding with feature clustering or DSFFC [41], correlation based feature selection or CFS [42], CON [42], particle swarm optimization search or PSO search [43], genetic search [44] and improved differential evolution based unsupervised feature selection or IMoDEFS [45] is provided in the paper. Classification accuracies on reduced datasets generated by CFS, CON, PSO search and genetic search are measured by various classifiers available at WEKA [46] tool while the same is collected from paper [41] for feature selection methods like FSFS, LSFS, MCFS and DSFFC. The experimental result shows the effectiveness of the proposed method.

The remaining part of the paper is organized as follows: some preliminary concepts of DE used in proposed method are described in Section II. Subsequently, detailed feature selection methodologies based on DE, experimental results and comparative performance analysis are provided in Sections II and III, respectively. Finally, Section IV holds the conclusion and final comments.

# II. THE DIFFERENTIAL EVOLUTION PRELIMINARIES

Initialization, mutation, recombination and selection are four basic steps of standard differential evolution or DE algorithm. The generations are executed sequentially until some termination criteria are satisfied (proposed work used exhaustion of maximum iteration as termination criteria).

## A. Initialization

In DE, initialization of Np real-valued vectors whose components represent D parameters of the optimization problem is the first step of search for global optimum in D directional search space. A generalized notation used to identify the  $i^{th}$  solution (real parameter vector) of the present generation G can be shown as:

$$\vec{X}_{i,G} = [x_{1,i,G}, x_{2,i,G} \dots x_{D,i,G}].$$

Given the decision parameter bounds,

 $\vec{X}_{max} = [x_{1,max}, x_{2,max} \dots x_{D,max}], \text{ and } \vec{X}_{min} = [x_{1,min}, x_{2,min} \dots x_{D,min}], \text{ the } j^{\text{th}} \text{ dimension of } i^{\text{th}} \text{ individual is initialized by Eq. (1).}$ 

$$x_{i,j} = x_{j,min} + rand_{i,j} \times (x_{j,max} - x_{j,min})$$
(1)

where  $rand_{i,j}$  is a uniformly distributed random number lying in the range [0, 1] and it is newly generated for each ordered pair (i, j).

### **B.** Mutation

Invited target vector is the term for any population member (say, *i*) of the current population, mutated with scaled difference vectors  $(\vec{X}_{r_{1,G}} - \vec{X}_{r_{2,G}})$  to produce a new mutant or *donor vector*. The indices  $r_1$  and  $r_2$ , sampled from  $\{1, 2, ..., Np\}$ , are different from the current index *i*. A scaling factor *F*, usually lying in the range [0.4, 2], scales the difference vector(s). Two well-known DE mutation strategies are listed in Eq. (2a) and (2b).

$$DE / rand / 1:: \vec{V}_{i,G} = \vec{X}_{r_1,G} + F(\vec{X}_{r_2,G} - \vec{X}_{r_3,G})$$
 (2a)

$$DE / best / 1:: \vec{V}_{i,G} = \vec{X}_{best,G} + F(\vec{X}_{r_2,G} - \vec{X}_{r_3,G})$$
(2b)

where  $r_1$ ,  $r_2$ , and  $r_3$  are mutually exclusive indices that are randomly selected from  $\{1, 2, ..., Np\}$ .

### C. Recombination

In DE, the crossover step aims to combine the individual components of the parent and the mutant vector into a single offspring commonly known as *trial vector*  $\vec{U}_{i,G} = [\boldsymbol{u}_{1,i,G}, \boldsymbol{u}_{2,i,G}, \dots \boldsymbol{u}_{D,i,G}]$ . DE primarily employs either *exponential* (two-point modulo) or *binomial* (uniform) crossover strategies. Generally, binomial crossover is preferred since it does away with the inherent representational bias in *n*-point crossover by simulating *D* random trials. Moreover, a recent work [35] attributing to the sensitivity of crossover to population size has reported the exponential variant to be more prone as compared to its binomial counterpart. Owing to the aforesaid observations, here we employ binomial crossover to form the trial vector.

In order to implement the binomial crossover, the control parameter *Crossover rate* (*Cr*) is set to a fixed value lying in the range [0, 1] and then *D* independent random numbers (between 0 and 1) are sampled uniformly and compared with *Cr* to decide which component is to be included in the trial vector. The components of the trial vector are computed using Eq. (3).

$$\boldsymbol{u}_{j,i,G} = \begin{cases} \boldsymbol{v}_{j,i,G}, \text{ if } rand_{i,j} < CR \text{ and } j = j_r, \\ \boldsymbol{x}_{j,i,G} \text{ otherwise} \end{cases}$$
(3)

where,  $j_r$  is a randomly chosen index from  $\{1, 2...D\}$  and

it ensures that at least one component from the mutant vector is present in the offspring produced.

### **D.** Selection

Finally, a selection process is performed through a one-to-one competition between the parent and the offspring to maintain a constant population size. The selection process can be defined using Eq. (4).

$$\vec{X}_{i,G+1} = \begin{cases} \vec{U}_{i,} & \text{if } f(\vec{U}_{i}) \leq f(\vec{X}_{i}), \\ X_{i,} & \text{otherwise} \end{cases}$$
(4)

where, f(.) is the objective function to be minimized.

### **III. DE BASED FEATURE SELECTION**

In the paper, the concepts of DE are used to select the most important features of the dataset that can fully characterize the overall system.

### A. Population Generation

As DE is a population based stochastic search algorithm, the initial population for proposed method is created at random. The dimension of population set is  $P \times N$  where P is the defined population size and N is the number of features in the dataset.

### **B. Encoded Solution Representation**

Binary string representation of potential solution is opted in this work. The length of the string is the same as the total number of features present in the dataset. Each encoded population member consists only of two values, where '1' means that index feature is present in current subset and '0' means that index feature is absent in current subset. So, a chromosome  $C_1$  of length K is represented as  $\{1 \ 0 \ 1 \ 1 \ ... \ 1 \ 0 \}$ .

## C. Mutation Strategy

While traditional 'vector difference based' mutation strategies are perfect for real values, this scheme is not suitable for the proposed work where population of binary strings is considered. To overcome this problem the proposed method uses hamming distance [47] and binary bitwise operation based mutation scheme. In this scheme, for the difference vector two distinct population members are selected from current population at unbiased manner. Then hamming distance is calculated among these two population members and a scaling parameter  $F \in [0.5, 2]$ is multiplied with it and its ceiling value is considered as the difference factor for proposed mutation scheme. Now from base vector a random string is generated, which has the same hamming distance of difference factor with the base vector.

## D. Recombination Strategy

Here, binomial recombination [21] strategy is used where each dimension of newly generated trial vector comes from the corresponding dimension of either base vector or mutant vector based on the control parameter Cr. The value of Cr is chosen either 0 or 1 at random and unique for each dimension of trial vector and finally the standard binomial recombination is opted.

## E. Set Dominance Relationship, Non-dominated Set and Pareto Front

Dominance Relationship: A solution  $X_1$  dominates other solution  $X_2$  and it is written as  $X_1 \ge X_2$  if both of the following conditions are satisfied:

- (1) The solution  $X_1$  is no worse than  $X_2$  with respect to all objective functions;
- (2) The solution  $X_1$  is strictly better than  $X_2$  with respect to at least one objective function.

Mathematically,  $X_1 \ge X_2$  iff  $f_i(X_1) \ge f_i(X_2)$  for all M objective functions  $f_1, f_2, ..., f_M$  and there exist at least one objective function  $f_j$  (for j = 1, 2, ..., M) for which  $f_j(X_1) > f_j(X_2)$ . Dominance relation is not reflexive and symmetric but transitive. Non-dominated set is the set among a set of solutions R that are not dominated by any member of the set R.

Strong dominance solution is the solution  $X_1$  which strongly dominates another solution  $X_2$ , i.e.,  $X_1 > X_2$  if solution  $X_1$  is strictly better than solution  $X_2$  in all Mobjective functions.

Algorithm 1 of proposed DE based feature selection method or DEFS is given below.

### Algorithm 1 DEFS $(U, N_P, F_V, CR_V, D, I_M)$

/\* U is the dataset used for feature selection,  $N_P$  is population size,  $F_V$  is the vector of [0.5 2] for scaling factor F,  $CR_V$  is the vector of [1 0] for recombination factor CR, D is the dimension of the dataset used and  $I_M$  is maximum permitted iteration \*/ 1: Begin 2: for  $i = 1... N_P do$ 3: for j = 1.. D do $x_i^j \leftarrow rand[0,1]$ 4: 5: end for 6: end for 7: for  $g=1..I_M$  do 8: **for**  $i = 1... N_P do$ Randomly generate two integers  $r_1, r_2(\mp i) \in$ 9:  $[1, N_P]$ 

10:  $F \leftarrow F_V(rand_i(length(F_V)))$ 

11:  $v_{i,g} \leftarrow x_{i,g} \otimes [F.hamming\_dist(x_{r_{1},g}, x_{r_{2},g})]$ 

12: end for

- 13: **for**  $i = 1.. N_P$  do
- 14:  $jrand \leftarrow [D.rand(0, 1)]$
- 15:  $CR \leftarrow CR_V(rand_i(length(CR_V)))$
- 16: **for** j = 1.. D do
- 17: if  $rand(0, 1) \leq CR$  or j = jrand then
- 18:  $u_{i,g}^j \leftarrow v_{i,g}^j$
- 19: **else**  $u_{i,q}^j \leftarrow x_{i,q}^j$
- 20: **end if**
- 21: end for
- 22: end for
- 23: **for** i = 1.. NP do
- 24: **if**  $f(U, u_{i,g}) > f(U, x_{i,g})$  then
- 25:  $x_{i,g+1} \leftarrow u_{i,g}$
- 26: else  $x_{i,g+1} \leftarrow x_{i,g}$
- 27: end if
- 28: end for
- 29: end for
- 30: **return** (*x*)
- 31: End procedure
- 32: Output: Reduct Set

## F. Objective Functions

The proposed bi-objective feature selection algorithm uses approximation accuracy of rough set theory and relational algebra based score as searching criteria for selecting the most relevant and noise-insensitive feature subset from a large feature set. To calculate lower bound approximation for any target set X with respect to an attribute subset P, universe of discourse U is partitioned into equivalence classes  $[x]_p$  using indiscernible relation IND(P), defined in Eq. (5).

$$IND(P) = \{(x,y) \in (|U| \times |U|) | \forall a \in P, f_a(x) = f_a(y) \quad (5)$$

where, f is the function that represents attribute value of an object. Similarly, equivalence classes  $[x]_{D}$  are formed using Eq. (5) for the subset D consisting of decision attributes. Thus, two different partitions U/P and U/D of equivalence classes  $[x]_p$  and  $[x]_p$  are obtained. Now, each class  $[x]_D$  in U/D is considered to be the target set X, i.e.,  $X \in U/D$ . The lower approximation PX of X under P is computed using Eq. (6), for all  $X \in U/D$  which contains the set of objects that positively belong to the target set X. The positive region  $POS_P(D)$  is obtained by taking the union of the lower approximations <u>PX</u> under P for all X in U/D, using Eq. (7), dependency value of D on P (i.e.,  $\gamma_{P}(D)$ ) is obtained using Equation 8 which signifies how much the decision attribute depends on the condition attribute set P. If D is fully dependent on P, i.e., if  $\gamma_P(D) = 1$ then P is the sufficient to represent the decision system and remaining attributes are irrelevant in the sense that

they do not contribute any significant information about the system.

$$\underline{P}X = \{x | [x]_{P} \subseteq X\}$$
(6)

$$POS_P(D) = \bigcup_{X \in U/D} \underline{P}X \tag{7}$$

$$\gamma_P(D) = \frac{|POS_P(D)|}{|U|} \tag{8}$$

The relational algebra operation division ( $\div$ ), defined in Definition 1, has been used to compute the second objective function of proposed method. For each present feature  $C_i$  in any population member,  $S(C_i)$  is calculated according to Eq. (9.)

$$S(C_i) = \prod_{C_i \cup D} (DS) \div \prod_D (DS)$$
(9)

Final score of any given population member is calculated by taking average of all individual  $C_i$  scores, where i=1,2,...,N.

Minimum score of  $C_i$  implies that there is a maximum number of objects having feature values similar to  $C_i$ , which can uniquely take the decisions. Thus, the population member with minimum average score is of maximum importance and so lower score implies higher possibility of becoming a member of reduct.

**DEFINITION 1:** Relational algebra operation division  $(\div)$  is a binary operation applied on two relations  $R_1(P)$  and  $R_2(Q)$  and produce another relation R(P-Q) where  $Q \subset P$ , where P, Q are set of attributes of  $R_1, R_2$ , respectively. So, R (i.e.,  $R_1 \div R_2$ ) contains set of all tuples t such that for any tuple  $t_1$  and  $t_2$  of  $R_1$  and  $R_2$ , respectively, following conditions hold.

Hence, to find most compact feature set first objective namely set approximation accuracy, is to 'be maximized' and second objective function relational algebra based score is to be minimized; in implementation negative of second objective is considered so now both objective values are to be maximized.

### **IV. EXPERIMENTAL RESULTS**

Extensive experiments are done to evaluate proposed feature selection method using some well-known machine learning datasets from UCI ML repository [38]. Details of datasets are given in Section IV-A and a performance comparison of proposed method with FSFS, LSFS and MCFS. DSFS is opted from [41] for comparison reason, results of IMODEFS [45] on those datasets are taken from [45]. For LSFS and MCFS, neighborhood size is taken as

ets

Dataset	Features	Samples	Class
Multiple features	649	2000	10
Isolet	617	6238	26
Spambase	57	4601	2
Ionosphere	34	351	2
Wdbc	30	569	2
Sonar	60	208	2
Spectf	44	80	2

default (=5). The details of these benchmark datasets, used classifiers and experimental results are given in this section. Parameters for proposed DE based feature selector is given underneath, population size is taken to be 100, maximum number of function evaluation is set to  $D \times 10^4$ , where D is the problem dimensionality; for comparative study all parameters are taken as respective algorithms in the literature.

### A. Used Dataset

The proposed method is validated using seven publicly available datasets, namely, Ionosphere, Sonar, Spambase, WDBC, Isolet, Multiple Features and Spectf, collected from UCI ML repository. A detailed description of all these datasets is given in (Table 1). The datasets are normalized using max-min normalization and all features are sealed into [0, 1] interval. These datasets are specifically chosen for some characteristics like large sample size (isolet, multiple features, spambase,) small feature size (ionosphere, sonar, spectf), two class (spambase, ionosphere, wdbc, sonar, spectf) and multiclass (multiple features, isolet) which are ideal to demonstrate effectiveness of the feature selection algorithm.

### **B. Classifiers Used**

Five classifiers, namely Naïve-Bayes (NB) [48], support vector machine (SVM) [49], K-nearest neighbors (k-NN) [48], AdaBoost\_Naive Bayes [50], C4.5 [51], are used to compare and contrast classification accuracy of the different feature selection algorithms.

SVM is used with RBF Kernel, k value of k-NN is set to the square root of sample size of data. Ten-fold crossvalidation is used for this classification performance evaluation. All these classifiers are used with WEKA tool.

### C. Evaluation Criteria

Five evaluation criteria are used for all these datasets for every classifier, as follows:

$$Acc = \frac{TP + TN}{TP + TN + FP + FN}$$

$$Recall = \frac{TP}{P} = \frac{TP}{TP + FN}$$

$$Fall\_out = \frac{FP}{N} = \frac{FP}{FP + TN}$$

$$Specificity = \frac{TN}{N} = \frac{TN}{FP + TN} = 1 - Fall\_out$$

$$F1\_score = \frac{2 \times TP}{2 \times TP + FP + FN}$$

$$TP \times TN - FP \times FN$$

 $MCC = \frac{TP \times TN - FP \times FN}{\sqrt{((TP + FP)(TP - FN)(TN + FP)(TN + FN))}}$ 

where TP, TN, FP, FN stand for true positives, true negatives, false positives, and false negatives, respectively.

MCC stands for Mathew's correlation coefficient. For all test datasets proposed method is executed 10 times and average values of those evaluation criteria's are reported here. For multiple features and Isolet dataset only accuracy is taken as evaluation criteria as these datasets are multi class in nature.

## D. Comparative Study

To show the effectiveness of the proposed method rigorous test has been done and the result of those test are listed in (Table 3) for comparison purpose. For these tests following parameter values are used: Population number = 100, Max Iteration = 500, CR = [0, 1], F = [2, 0.5].

Comparative accuracy for different degree of proposed feature selection method and other methods are given in Tables 2–6. Each entry of the table is average taken over 10 independent runs.

 Table 2. Performance comparison on Ionosphere and Sonar dataset

			Ionosphere					Sonar					
		NB	SVM	K-NN	Boosting	C4.5	NB	SVM	k-NN	Boosting	C4.5		
	Accuracy (%)	73.70	91.80	75.41	85.93	80.10	70.83	80.24	68.51	77.16	70.11		
	Recall	0.740	0.920	0.756	0.863	0.810	0.712	0.808	0.692	0.779	0.702		
FOFO	Fallout	0.260	0.080	0.246	0.142	0.200	0.289	0.202	0.317	0.231	0.298		
FSFS	Specificity	0.740	0.920	0.754	0.858	0.800	0.712	0.798	0.683	0.769	0.702		
	F1 score	0.740	0.920	0.756	0.860	0.800	0.712	0.804	0.689	0.775	0.702		
	MCC	0.480	0.840	0.510	0.721	0.610	0.423	0.606	0.375	0.548	0.404		
	Accuracy (%)	76.80	91.40	84.67	88.83	82.90	71.88	81.01	67.98	75.67	75.25		
LSFS	Recall	0.770	0.920	0.851	0.891	0.830	0.721	0.817	0.683	0.760	0.760		
	Fallout	0.230	0.090	0.153	0.114	0.170	0.279	0.192	0.317	0.240	0.240		
	Specificity	0.770	0.910	0.847	0.886	0.830	0.721	0.808	0.683	0.760	0.760		
	F1 score	0.770	0.920	0.849	0.889	0.830	0.721	0.813	0.683	0.760	0.760		
	MCC	0.540	0.830	0.698	0.778	0.660	0.442	0.625	0.365	0.519	0.519		
	Accuracy (%)	87.90	94.20	82.11	90.46	88.20	67.36	82.45	70.14	77.21	73.12		
	Recall	0.880	0.940	0.824	0.909	0.890	0.683	0.827	0.702	0.779	0.740		
MCFS	Fallout	0.120	0.060	0.177	0.097	0.120	0.327	0.173	0.298	0.231	0.269		
MCF5	Specificity	0.880	0.940	0.823	0.903	0.880	0.673	0.827	0.702	0.769	0.731		
	F1 score	0.880	0.940	0.824	0.906	0.880	0.679	0.827	0.702	0.775	0.737		
	MCC	0.760	0.890	0.647	0.812	0.770	0.356	0.654	0.404	0.548	0.471		
	Accuracy (%)	89.10	94.10	82.54	90.85	87.50	69.42	82.21	70.83	79.09	71.01		
	Recall	0.890	0.940	0.829	0.909	0.880	0.702	0.827	0.721	0.798	0.712		
DSFFC	Fallout	0.110	0.060	0.176	0.091	0.130	0.308	0.183	0.279	0.212	0.289		
DSFFC	Specificity	0.890	0.940	0.824	0.909	0.880	0.692	0.817	0.721	0.789	0.712		
	F1 score	0.890	0.940	0.826	0.909	0.880	0.699	0.823	0.721	0.794	0.712		
	MCC	0.780	0.890	0.652	0.818	0.760	0.394	0.644	0.442	0.587	0.423		

### Table 2. Continued

				Ionospher	·e				Sonar		
		NB	SVM	K-NN	Boosting	C4.5	NB	SVM	k-NN	Boosting	C4.5
	Accuracy (%)	77.300	78.60	79.88	80.00	68.30	60.12	59.35	70.11	68.25	67.00
	Recall	0.780	0.790	0.801	0.801	0.630	0.606	0.596	0.702	0.683	0.673
CFS	Fallout	0.230	0.220	0.200	0.200	0.370	0.394	0.404	0.298	0.317	0.327
CFS	Specificity	0.770	0.780	0.800	0.800	0.630	0.606	0.596	0.702	0.683	0.673
	F1 score	0.780	0.790	0.801	0.801	0.630	0.606	0.596	0.702	0.683	0.673
	MCC	0.550	0.570	0.601	0.601	0.27	0.212	0.192	0.404	0.365	0.346
	Accuracy (%)	67.60	63.20	70.00	72.35	63.00	61.29	63.55	69.53	62.39	65.00
	Recall	0.680	0.630	0.703	0.726	0.630	0.615	0.644	0.702	0.625	0.654
CON	Fallout	0.320	0.370	0.301	0.278	0.370	0.385	0.365	0.308	0.375	0.346
CON	Specificity	0.680	0.630	0.699	0.722	0.630	0.615	0.635	0.692	0.625	0.654
	F1 score	0.680	0.630	0.701	0.724	0.630	0.615	0.641	0.699	0.625	0.654
	MCC	0.360	0.270	0.402	0.447	0.270	0.231	0.279	0.394	0.250	0.308
	Accuracy (%)	70.00	70.30	73.93	78.05	73.00	70.00	69.53	62.39	76.55	70.33
	Recall	0.700	0.710	0.743	0.783	0.730	0.702	0.702	0.625	0.769	0.712
PSO	Fallout	0.300	0.300	0.261	0.222	0.270	0.298	0.308	0.375	0.231	0.298
search	Specificity	0.700	0.700	0.739	0.778	0.730	0.702	0.692	0.625	0.769	0.702
	F1 score	0.700	0.710	0.741	0.781	0.730	0.702	0.699	0.625	0.769	0.708
	MCC	0.400	0.410	0.482	0.561	0.460	0.404	0.394	0.250	0.539	0.414
	Accuracy (%)	75.300	79.00	78.09	72.33	72.00	65	63.11	70.29	61.00	56.09
	Recall	0.760	0.790	0.794	0.726	0.720	0.654	0.635	0.712	0.615	0.577
Genetic	Fallout	0.250	0.210	0.210	0.278	0.280	0.346	0.365	0.298	0.394	0.433
search	Specificity	0.750	0.790	0.790	0.722	0.720	0.654	0.635	0.702	0.606	0.567
	F1 score	0.760	0.790	0.792	0.724	0.720	0.654	0.635	0.708	0.612	0.574
	MCC	0.510	0.58	0.584	0.447	0.440	0.308	0.269	0.414	0.221	0.144
	Accuracy (%)	90.10	93.70	83.87	91.28	90.60	68.77	84.18	75.05	81.83	73.99
	Recall	0.900	0.940	0.841	0.915	0.910	0.692	0.846	0.760	0.827	0.740
Madees	Fallout	0.100	0.060	0.160	0.086	0.090	0.308	0.154	0.250	0.183	0.260
MoDEFS	Specificity	0.900	0.940	0.840	0.914	0.910	0.692	0.846	0.750	0.817	0.740
	F1 score	0.900	0.940	0.841	0.915	0.910	0.692	0.846	0.756	0.823	0.740
	MCC	0.810	0.88	0.681	0.829	0.820	0.385	0.692	0.510	0.644	0.481
	Accuracy (%)	89.70	93.10	84.89	84.11	87.10	73.56	83.65	79.98	76.65	79.12
	Recall	0.900	0.930	0.851	0.846	0.870	0.74	0.837	0.808	0.769	0.798
Duou o 1	Fallout	0.100	0.070	0.153	0.159	0.130	0.26	0.164	0.202	0.231	0.212
Proposed	Specificity	0.900	0.930	0.847	0.841	0.870	0.74	0.837	0.798	0.769	0.789
	F1 score	0.900	0.930	0.849	0.843	0.870	0.74	0.837	0.804	0.769	0.794
	MCC	0.800	0.860	0.698	0.687	0.740	0.481	0.673	0.606	0.539	0.587

				Spam			WDBC					
		NB	SVM	k-NN	Boosting	C4.5	NB	SVM	k-NN	Boosting	C4.5	
	Accuracy (%)	66.70	79.00	80.81	66.85	77.00	91.11	94.41	93.22	94.22	95.5	
	Recall	0.670	0.790	0.808	0.669	0.770	0.912	0.947	0.933	0.944	0.95	
ESES	Fallout	0.330	0.210	0.192	0.332	0.230	0.088	0.056	0.067	0.056	0.04	
FSFS	Specificity	0.670	0.790	0.808	0.668	0.770	0.912	0.944	0.933	0.944	0.95	
	F1 score	0.670	0.790	0.808	0.669	0.770	0.912	0.946	0.933	0.944	0.95	
	MCC	0.330	0.580	0.617	0.337	0.540	0.824	0.891	0.866	0.888	0.91	
	Accuracy (%)	69.30	83.80	82.86	69.28	69.10	93.71	96.87	95.87	95.85	90.2	
	Recall	0.690	0.840	0.827	0.693	0.690	0.940	0.972	0.961	0.961	0.90	
LCEC	Fallout	0.310	0.160	0.173	0.307	0.310	0.063	0.032	0.042	0.042	0.09	
LSFS	Specificity	0.690	0.840	0.827	0.693	0.690	0.937	0.968	0.958	0.958	0.90	
	F1 score	0.690	0.840	0.827	0.693	0.690	0.939	0.970	0.960	0.960	0.90	
	MCC	0.390	0.680	0.654	0.386	0.380	0.877	0.940	0.919	0.919	0.80	
	Accuracy (%)	65.30	80.00	82.27	65.25	72.60	93.39	96.68	96.22	95.11	88.6	
	Recall	0.650	0.800	0.823	0.653	0.730	0.937	0.968	0.965	0.954	0.88	
MOEG	Fallout	0.350	0.200	0.177	0.347	0.270	0.067	0.031	0.039	0.049	0.11	
MCFS	Specificity	0.650	0.800	0.823	0.653	0.730	0.933	0.968	0.961	0.951	0.88	
	F1 score	0.650	0.800	0.823	0.653	0.730	0.935	0.968	0.963	0.953	0.88	
	MCC	0.310	0.600	0.646	0.305	0.450	0.87	0.937	0.926	0.905	0.77	
	Accuracy (%)	75.60	86.70	84.31	75.71	69.90	94.34	96.82	95.73	96.22	91.2	
	Recall	0.760	0.870	0.844	0.757	0.700	0.944	0.968	0.958	0.965	0.91	
	Fallout	0.240	0.130	0.157	0.243	0.300	0.056	0.032	0.042	0.039	0.08	
DSFFC	Specificity	0.760	0.870	0.843	0.757	0.700	0.944	0.968	0.958	0.961	0.91	
	F1 score	0.760	0.870	0.843	0.757	0.700	0.944	0.968	0.958	0.963	0.91	
	MCC	0.510	0.730	0.687	0.515	0.400	0.888	0.937	0.916	0.926	0.82	
	Accuracy (%)	76.30	79.10	78.59	70.00	70.10	90.00	91.22	93.31	92.56	92.3	
	Recall	0.760	0.790	0.786	0.700	0.700	0.902	0.916	0.933	0.926	0.92	
959	Fallout	0.240	0.210	0.214	0.300	0.300	0.099	0.088	0.067	0.074	0.07	
CFS	Specificity	0.760	0.790	0.786	0.700	0.700	0.901	0.912	0.933	0.926	0.92	
	F1 score	0.760	0.790	0.786	0.700	0.700	0.902	0.914	0.933	0.926	0.92	
	MCC	0.530	0.580	0.572	0.400	0.400	0.803	0.828	0.866	0.852	0.84	
	Accuracy (%)	70.00	70.00	69.03	68.95	65.10	88.59	89.56	90.23	91.69	89.9	
	Recall	0.700	0.700	0.691	0.690	0.650	0.888	0.898	0.905	0.919	0.90	
	Fallout	0.300	0.300	0.31	0.310	0.350	0.113	0.105	0.098	0.084	0.09	
CON	Specificity	0.700	0.700	0.69	0.690	0.650	0.887	0.895	0.902	0.916	0.90	
	F1 score	0.700	0.700	0.691	0.690	0.650	0.888	0.896	0.903	0.917	0.90	
	MCC	0.400	0.400	0.381	0.379	0.300	0.775	0.793	0.807	0.835	0.80	
	Accuracy (%)	73.50	79.10	81.00	72.35	76.00	91.29	92.35	91.36	90.25	89.8	
	Recall	0.740	0.790	0.810	0.724	0.760	0.916	0.926	0.916	0.905	0.90	
PSO	Fallout	0.270	0.210	0.190	0.277	0.240	0.088	0.077	0.088	0.098	0.10	
search	Specificity	0.740	0.790	0.810	0.277	0.760	0.912	0.923	0.912	0.902	0.89	
	F1 score	0.740	0.790	0.810	0.724	0.760	0.914	0.924	0.914	0.903	0.90	
	MCC	0.470	0.580	0.620	0.447	0.520	0.828	0.849	0.828	0.807	0.80	

Table 3. Performance comparison on Spam and WDBC dataset

				Spam					WDBC		
		NB	SVM	k-NN	Boosting	C4.5	NB	SVM	k-NN	Boosting	C4.5
	Accuracy (%)	70.20	62.10	63.39	69.99	70.10	90.29	90.35	89.39	88.36	85.78
	Recall	0.700	0.620	0.634	0.700	0.700	0.905	0.905	0.895	0.884	0.860
Genetic	Fallout	0.300	0.380	0.366	0.300	0.300	0.098	0.095	0.106	0.116	0.141
search	Specificity	0.700	0.620	0.634	0.700	0.700	0.902	0.905	0.894	0.884	0.859
	F1 score	0.700	0.620	0.634	0.700	0.700	0.903	0.905	0.895	0.884	0.860
	MCC	0.410	0.240	0.268	0.400	0.400	0.807	0.81	0.789	0.768	0.719
	Accuracy (%)	76.10	87.80	85.47	75.99	91.80	93.18	96.38	95.73	96.27	95.20
	Recall	0.760	0.880	0.855	0.760	0.920	0.933	0.965	0.958	0.965	0.954
MADEEC	Fallout	0.240	0.120	0.145	0.240	0.080	0.067	0.035	0.042	0.039	0.049
IMoDEFS	Specificity	0.760	0.880	0.855	0.760	0.920	0.933	0.965	0.958	0.961	0.951
	F1 score	0.760	0.880	0.855	0.760	0.920	0.933	0.965	0.958	0.963	0.953
	MCC	0.520	0.760	0.710	0.520	0.840	0.866	0.93	0.916	0.926	0.905
	Accuracy (%)	78.90	92.50	91.22	88.56	90.70	95.37	85.66	96.89	92.23	95.72
	Recall	0.790	0.080	0.913	0.886	0.910	0.954	0.859	0.972	0.923	0.958
Duranal	Fallout	0.210	0.930	0.088	0.114	0.090	0.046	0.144	0.032	0.078	0.042
Proposed	Specificity	0.790	0.930	0.912	0.886	0.910	0.954	0.856	0.968	0.923	0.958
	F1 score	0.790	0.930	0.912	0.886	0.910	0.954	0.858	0.97	0.923	0.958
	MCC	0.580	0.850	0.825	0.771	0.810	0.909	0.715	0.94	0.845	0.916

### Table 3. Continued

Table 4. Performance comparison (accuracy, %) on Spectf and Multiple features dataset

			Spectf		Multiple features						
	NB	SVM	k-NN	Boosting	C4.5	NB	SVM	K-NN	Boosting	C4.5	
FSFS	73.63	73.38	66.00	65.50	65.50	96.00	97.90	94.49	96.54	91.00	
LSFS	72.79	74.00	69.63	69.00	62.33	94.00	97.70	93.02	96.15	92.00	
MCFS	72.13	71.88	66.38	72.75	63.21	96.00	98.10	95.58	97.06	94.00	
DSFFC	79.75	76.88	68.13	76.88	76.12	94.00	98.40	95.61	96.22	91.00	
CFS	70.23	71.11	70.21	69.22	60.29	92.00	94.60	93.99	96.55	92.00	
CON	70.11	63.33	61.39	65.55	60.00	93.00	94.60	93.99	96.55	92.00	
PSO search	71.11	72.19	70.11	61.15	65.59	92.00	90.20	93.55	90.00	90.00	
Genetic search	61.00	62.00	63.35	59.99	60.10	90.00	91.50	88.92	89.99	90.00	
IMoDEFS	85.75	73.88	66.8	74.63	66.25	95.00	98.20	95.99	96.21	95.00	
Proposed	79.20	76.69	72.50	72.35	79.00	99.00	97.20	96.44	97.84	97.00	

Table 5. Performance comparison (accuracy, %) on Isolet dataset

			Isolet		
	NB	SVM	k-NN	Boosting	C4.5
FSFS	66.00	88.20	71.42	65.78	61.70
LSFS	76.00	93.00	82.60	75.53	76.60
MCFS	82.00	95.80	87.99	81.99	78.30
DSFFC	84.00	95.30	86.19	84.82	79.60
CFS	80.00	82.30	83.69	84.81	81.20
CON	80.00	78.20	70.11	76.25	71.20
PSO search	80.00	81.30	82.55	83.92	69.00
Genetic search	70.00	68.20	71.55	68.99	75.30
IMoDEFS	86.00	95.50	87.79	86.03	80.70
Proposed	86.00	96.00	89.46	85.45	85.00

From Table 6, it is clear that proposed method works better than FSFS, LSFS, MCFS, DSFFC, CFS, CON, PSO search, Genetic search, and is a close contender of IMoDEFS method and in some cases outperforms them.

The experiments are carried out in MATLAB using workstation having 5 GHz octa-core CPU and 32 GB of RAM.

## **V. CONCLUSIONS**

In this work, an algorithm for feature selection using modified binary differential evolution is proposed. For this purpose two objective functions, namely division based

	Ionosphere	Sonar	Spam	Wdbc	Isolet	Multiple features	Spectf
FSFS	0	0	0	0	0	0	0
LSFS	0	0	0	1	0	0	0
MCFS	1	0	0	0	0	0	0
DSFFC	0	0	0	0	0	0	3
CFS	0	0	0	0	0	0	0
CON	0	0	0	0	0	0	0
PSO search	0	0	0	0	0	0	0
Genetic search	0	0	0	0	0	0	0
IMoDEFS	3	2	1	1	1	1	0
Proposed	1	3	4	3	4	4	2

Table 6. Number of times best results are obtained by each of the above mentioned feature selection algorithm

feature score and set lower boundary approximation, are introduced to be used along with proposed global version of binary differential evolution algorithm. Effectiveness of proposed algorithm is shown by comparing it with other several state of the art feature selection methods by means of different statistical accuracy measures. Computational complexity of proposed method is relatively higher than other compared algorithms but on average proposed method gives significantly better result. The proposed method used Pareto-based approach to tackle two objective optimization, thus there are several other approaches to tackle this kind of problem in future applicability of those methods along with proposed differential evolution algorithm. Finally, a detailed sensitivity analysis of the feature selection technique with various algorithmic parameter need to be done in future.

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